Guided Notes – 3.2 Domain and Range

LEARNING OBJECTIVES

In this section, you will:

- Find the domain of a function defined by an equation.
- Graph a piecewise-defined function.

FINDING THE DOMAIN OF A FUNCTION DEFINED BY AN EQUATION

• As a review, write the 4 conventions of interval notation as described in your textbook:

1. 2. 3. 4.

Try It: Read Example 1 in the text, then answer the following.

Find the domain of the function: $\{(-5,4), (0,0), (5,-4), (10,-8), (1,-12)\}$

- Write the 3-step process for finding the domain, given a function written in equation form.
 - 1.
 - 2.
 - 3.

Try It: Read Example 2 in the text, then answer the following.

Find the domain of the function: $f(x) = 5 - x + x^3$.

• Write the 3-step process for finding the domain, given a function written in equation form that includes a fraction.

1.

- 2.
- 3.
- Try It: Read Example 3 in the text, then answer the following.

Find the domain of the function $f(x) = \frac{1+4x}{2x-1}$.

- Write out the 3-step process for finding the domain, given a function written in equation form including an even root.
 - 1.
 - 2.

Try It: Read Example 4 in the text, then answer the following.

Find the domain of the function $f(x) = \sqrt{5 + 2x}$.

USING NOTATIONS TO SPECIFY DOMAIN AND RANGE

Study Figure 5 in your textbook section which compares inequality, set-builder, and interval notation.

	Inequality Notation	Set-Builder Notation	Interval Notation
	$5 < h \le 10$		
4 $			[5, 10)
$4 \diamond$ $ \qquad \qquad \phi >$ 5 10	5 < h < 10	$\{ h \mid 5 < h < 10 \}$	
4 4 + + + + + + + + +		$\{ h \mid h < 10 \}$	(−∞,10)
			[10,∞)
→ → + + → → 5 10	All real numbers		

• Write out the 4-step process for describing the set of values using interval notation, given a line graph.

- 2.
- 3.
- 4.

Try It: Read Example 5 in the text, then answer the following.

Given this figure, specify the graphed set in

a. words



b. set-builder notation



c. interval notation

FINDING DOMAIN AND RANGE FROM GRAPHS

Try It: Read Examples 6 and 7 in the text, then answer the following.

Given Figure 12, identify the domain and range using interval notation.



FINDING DOMAINS AND RANGES OF THE TOOLKIT FUNCTIONS

Study the table in your textbook section under "Finding Domains and Ranges of the Toolkit Functions".

• Fill in the domains and ranges of the toolkit functions, using interval notation.

TOOLKIT FUNCTIONS				
Name	Domain	Range		
Constant				
Identity				
Absolute Value				

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Quadratic	
Cubic	
Reciprocal	
Reciprocal Squared	
Square Root	
Cube Root	

• Write out the 4-step process for determining the domain and range, given the formula for a function.

1.
2.
3.

4.

Try It: Read Examples 8, 9, and 10 in the text, then answer the following.

Find the domain and range of $f(x) = -\sqrt{2-x}$.

GRAPHING PIECEWISE-DEFINED FUNCIONS

Study the box in your textbook section titled "piecewise function."

• State the definition of a piecewise function below.

- Write out the 3 step process for writing the formula and identifying the domain for each interval, given a piecewise function.
 - 1.
 - 2.
 - 3.
- Write out the 2 step process for sketching a graph, given a piecewise function.
 - 1.
 - 2.

Try It: Read Example 8 in the text, then answer the following.

Graph the following piecewise function.

$$f(x) = \begin{cases} x^3 & \text{if } x < -1 \\ -2 & \text{if } -1 < x < 4 \\ \sqrt{x} & \text{if } x > 4 \end{cases}$$

